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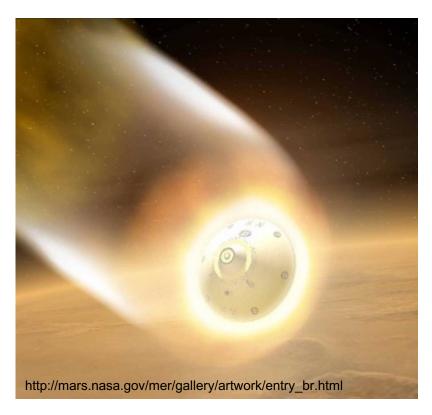
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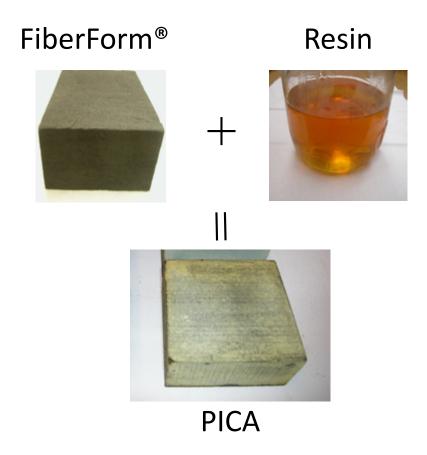
Ablation WS, 2017 Bozeman, MT

Ablative Thermal Protection Systems



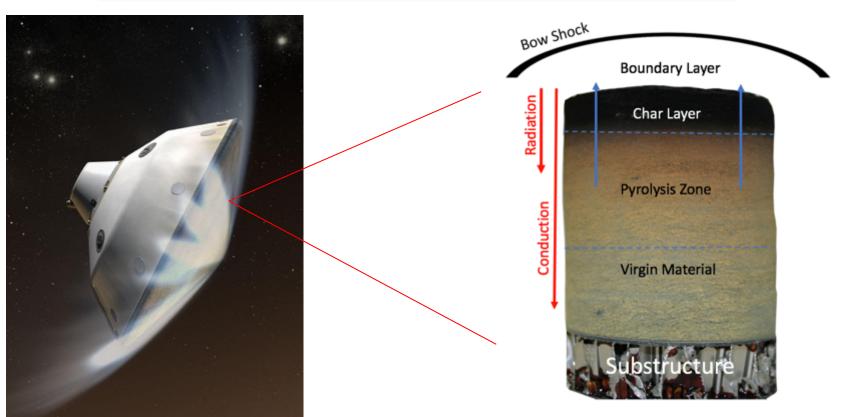


Artist rendering of MSL entry



Material Design and Modeling



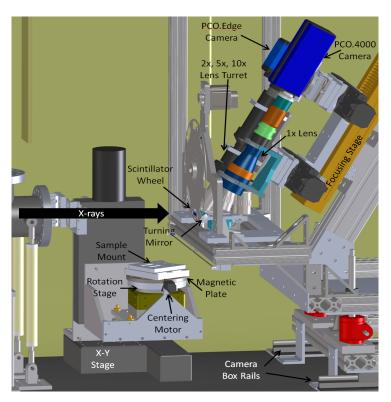


X-ray micro-tomography





- Advanced Light Source (ALS) at the Lawrence Berkeley Natl. Laboratory
- Synchrotron electron accelerator used to produce 14KeV X-rays
- Used for many research areas, including optics, chemical reaction dynamics, biological imaging, and X-ray micro-tomography.

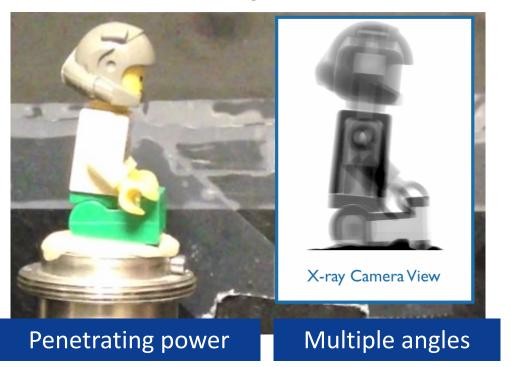


http://www2.lbl.gov/MicroWorlds/ALSTool

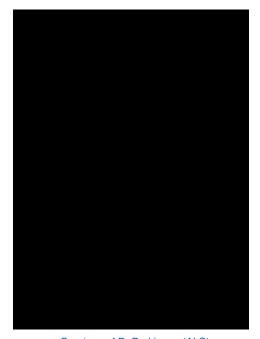
X-ray micro-tomography



Collect X-ray images of the sample as you rotate it through 180°



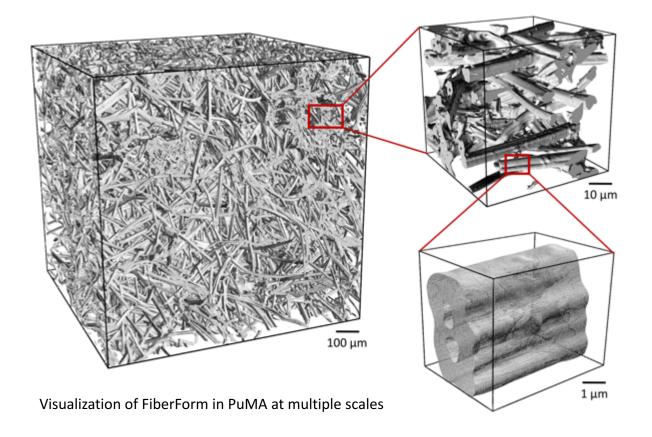
Use this series of images to "reconstruct" the 3D object



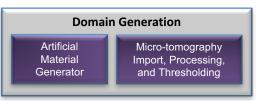
Courtesy of D. Parkinson (ALS)

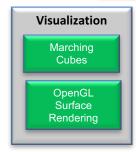
X-ray micro-tomography



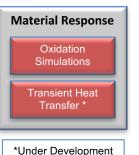


Porous Materials Analysis (PuMA)





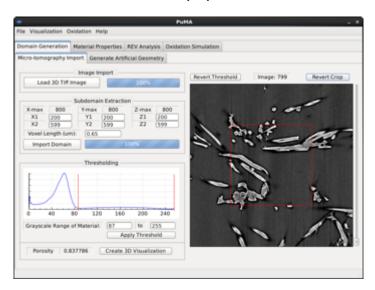




Technical Specifications



- Written in C++
- GUI built on QT
- Visualization module based on OpenGL
- Parallelized using OpenMP for shared memory systems



Tortuosity Factors



- Quantifies a materials resistance to a diffusive flux
- Important in modeling diffusion/reaction systems – such as ablative TPS response

$$\eta = \varepsilon \, \frac{D_{ref}}{D_{eff}}$$

- $\eta = \text{tortuosity factors}$
- $\varepsilon = \text{porosity}$
- D_{ref} = reference diffusion coefficient
- $D_{eff} = \text{effective diffusion coefficient}$



Surface rendering of FiberForm tomography in PuMA V2.1. Visualization contains ≈ 500 million triangles.

Knudsen Number



Non-dimensional number which defines the diffusion regime

$${\rm Kn}=rac{ar{\lambda}}{l_D}=rac{{
m Mean \ Free \ Path}}{{
m Characteristic \ Length}}$$

• Continuum: Kn << 1

• Transitional: $Kn \approx 1$

Rarified: Kn >> 1

Low Knudsen High Knudsen

2D diffusivity simulations using a random walk method in PuMA. Particle paths are visualized in red.

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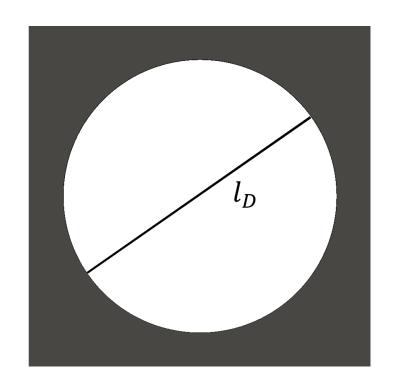
Reference Diffusion Coefficient



• D_{ref} = reference diffusion coefficient

Continuum	Free Molecular
$D_{ref} = D_{bulk}$	D_{bulk} does not exist

- $D_{bulk} = \frac{1}{3} \bar{v}\bar{\lambda}$, which is undefined as the mean free path approaches infinity
- D_{ref} therefore must be based on a length scale. In this case, the Diffusion coefficient through a capillary of diameter l_{D}



$$\bar{v}$$
 = mean thermal velocity $\bar{\lambda}$ = mean free path

Bosanquet Approximation

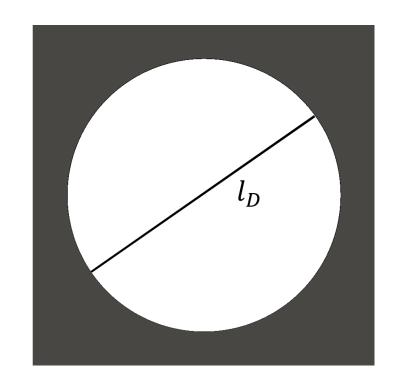


• Used to approximate D_{ref} based on known values for D_h and D_k . [1]

$$\frac{1}{D_{ref}} = \frac{1}{D_b} + \frac{1}{D_k}$$

• Rewritten for single species diffusion in a capillary, D_{ref} becomes [2]

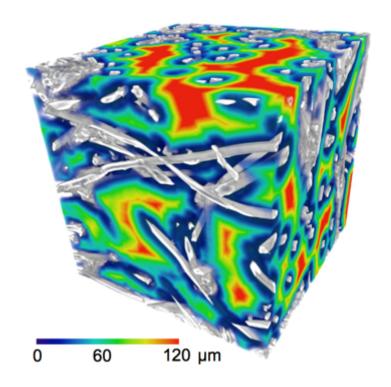
$$D_{ref} = \frac{1}{3} \, \bar{v} \, \left(\frac{\bar{\lambda} \, l_D}{\bar{\lambda} + l_D} \right)$$



Choice of Length Scale



- 1. Define l_D based on an approximate geometric length scale for the material. Typically $\frac{4\varepsilon}{S}$ or mean intercept length. (Tomadakis, Lachaud, Geodict)
- 2. Define l_D after the simulations are complete as the value which makes the tortuosity factor vs. Knudsen number plot converge to a single value. (Zalc)



Pore size distribution, computed in GeoDict, of FiberForm.

Length Scale Option #1



Define l_D based on an approximate geometric length scale for the material. Typically $\frac{4\varepsilon}{S}$ or mear intercept length. (Tomadakis, Lachaud, Geodict, PuMA)

- Most often used in the literature and software
- Requires values of η_b , η_k and l_D in order to apply the Bosanquet approximation
- η is no longer a purely geometrical property, as it is now a function of the Knudsen number
- Since η_b had no physical meaning without l_D , this can produce confusing results of η_k < 1

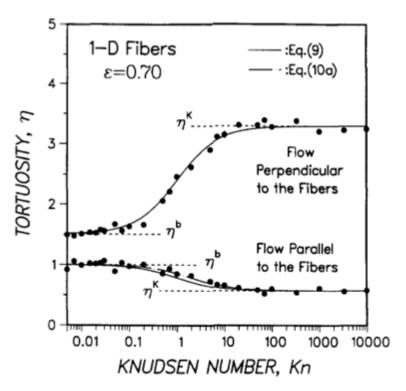


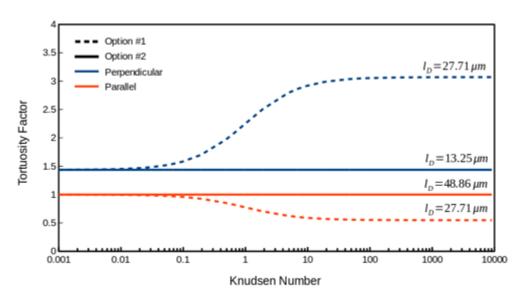
Figure from Tomadakis, 1993

Length Scale Option #2



Define l_D after the simulations are complete as the value which makes the tortuosity vs. Knudsen number plot converge to a single value. (Zalc, PuMA)

- Requires only one value of η and a computed length scale, l_D , in order to apply the Bosanquet approximation
- η is now longer a purely geometrical property, no longer a function of Kn
- Easier to understand and implement

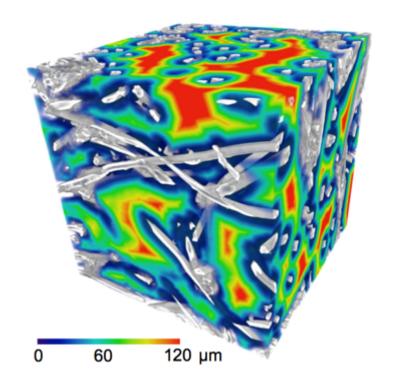


Tortuosity factor vs Knudsen Number for 1D fibers, computed in PuMA, showing the parallel and perpendicular tortuosity factors for Option #1 and Option #2

Choice of Length Scale



- 1. Define l_D based on an approximate geometric length scale for the material. Typically $\frac{4\varepsilon}{S}$ or mean intercept length. (Tomadakis, Lachaud, Geodict)
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Pore size distribution, computed in GeoDict, of FiberForm.

Applying Tortuosity Factors



• Used to compute D_{eff} within a porous media, with known tortuosity factor, η , known length scale, l_D , and known gas properties.

$$D_{eff} = \varepsilon \, \frac{D_{ref}}{\eta}$$

• Using Bosanquet approximation to approximate D_{ref} , the equation becomes

$$D_{eff} = \frac{\varepsilon}{3\eta} \; \bar{v} \left(\frac{\bar{\lambda} l_D}{\bar{\lambda} + l_D} \right)$$



Surface rendering of FiberForm tomography in PuMA V2.1. Visualization contains ≈ 500 million triangles.

Numerical Methods



Continuum

- Can be solved using typical numerical methods such as finite volume and finite difference
- 1. Geodict Explicit Jump Solver
- 2. PuMA Explicit Jump Solver
- TauFactor Finite Volume solver

MATH 2 MARKET

Rarified

- Must be solved using particle methods to account for Knudsen effects
- 1. PuMA Random walk solver
- Geodict Random walk solver (Knudsen regime)
- SPARTA Direct Simulation Monte Carlo





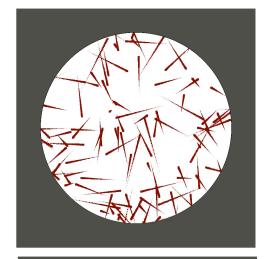


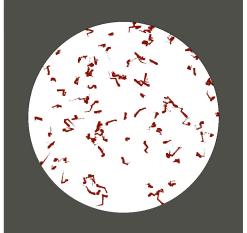
Random Walk Solver

- Particle method for solving diffusion
- Velocity and mean path for each particle based on exponential distribution
- Diffuse reflections are used for surface collisions
- Symmetric boundary conditions

$$D_{eff_i} = \frac{\langle \xi^2 \rangle}{2t}$$

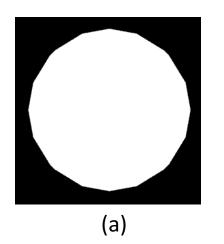
- $\langle \xi^2 \rangle$ is the mean square displacement of the particles
- Mean thermal velocity, \bar{v} , and mean free path, $\bar{\lambda}$, are imposed to simulate the desired gas species and conditions.

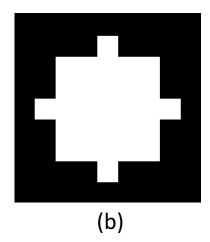




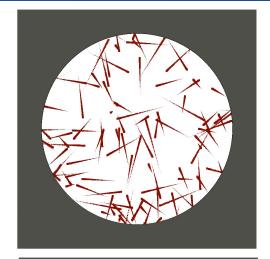
Wall Collisions

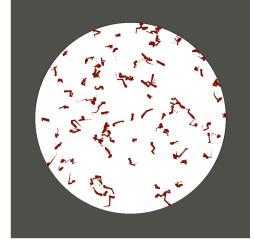
- Diffuse reflections used for surface collisions
- Collision detection can be based on isosurface or cuberille grid





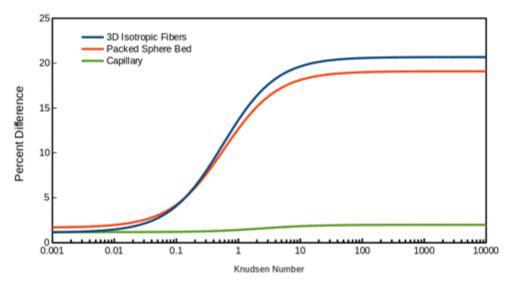
Isosurface (a) and cuberille (b) approximations of a cylinder with radius 3 voxels.



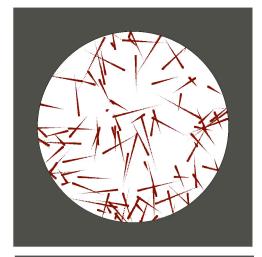


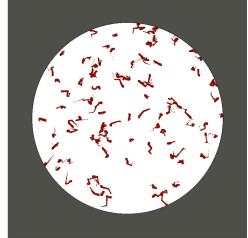
Wall Collisions

- Diffuse reflections used for surface collisions
- Collision detection can be based on isosurface or cuberille grid



Percent difference (isosurface vs cuberille) vs Knudsen number for three different ideal geometries

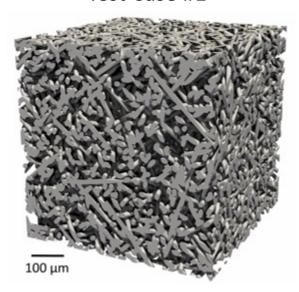




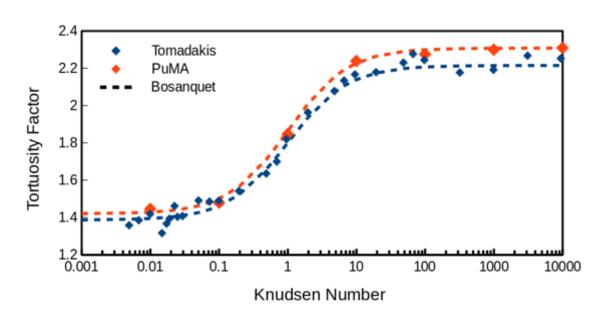
Comparison to Literature



Test Case #1



- 3D Fibers, 512³
- Intersecting, isotropic
- 0.6 porosity

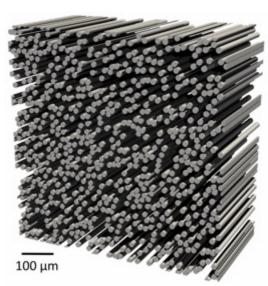


The 5% error is likely due to the limitations of computing in 1993. Simulations by Tomadakis were using only 200 particles and likely on a small dataset. The PuMA simulations were run on 200,000 particles for a total walk length of 10,000 times the domain length

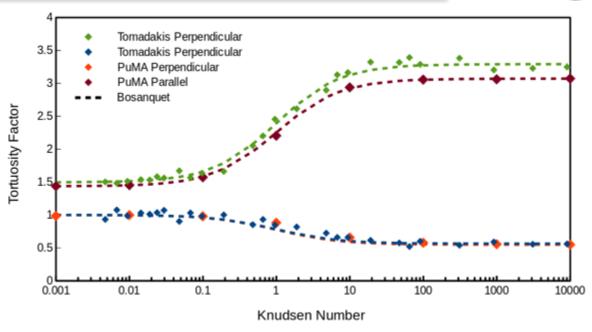
Comparison to Literature



Test Case #2



- 1D Fibers, 512 x 512 x 256
- Non intersecting
- 0.7 porosity

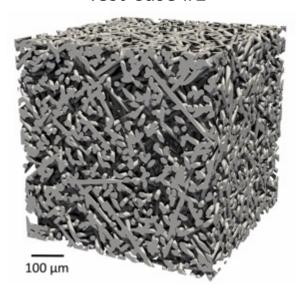


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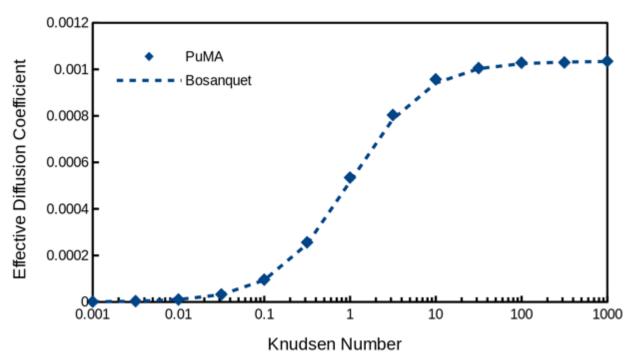
Bosanquet Analysis



Test Case #1



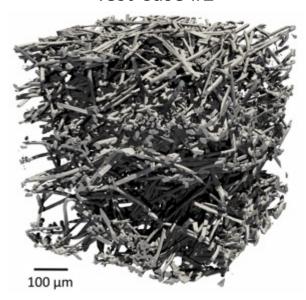
- 3D Fibers, 512³
- Intersecting, isotropic
- 0.6 porosity



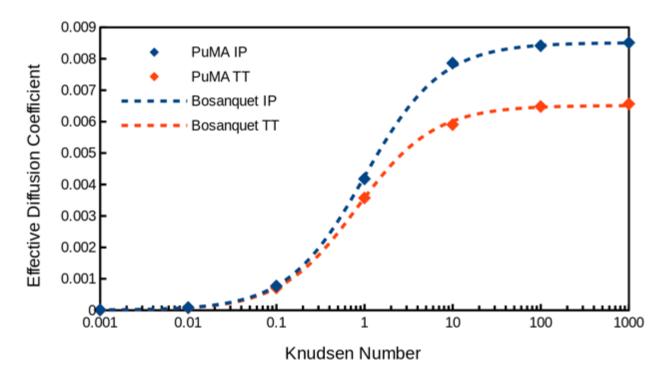
Bosanquet Analysis



Test Case #2



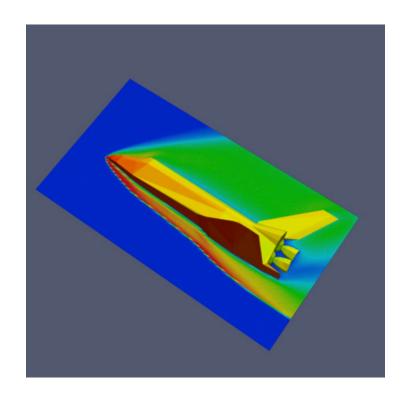
- FiberForm, 0.8 mm³
- Transverse isotropic
- 0.89 porosity



Direct Simulation Monte Carlo



- DSMC is a particle method to simulate transitional and rarified flows with high fidelity
- Very computationally expensive, preventing large or frequent simulations
- DSMC diffusion simulations conducted in SPARTA, developed at Sandia National Labs.
- Pressure varied to change the mean free path, and therefore the Knudsen number
- Used as a verification case for the random walk method

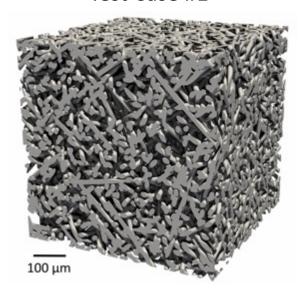


DSMC simulation of transitional flow over the Space Shuttle. Sparta.sandia.gov

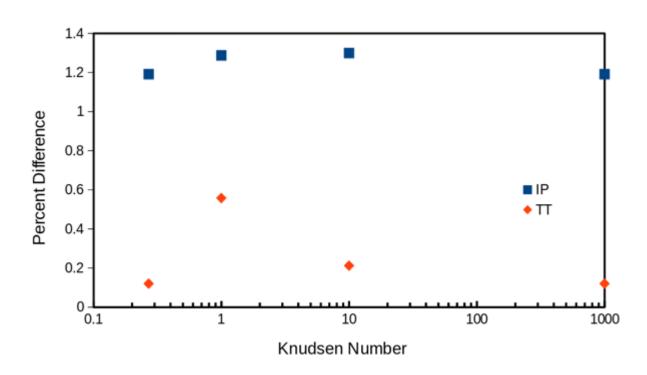
Direct Simulation Monte Carlo



Test Case #1



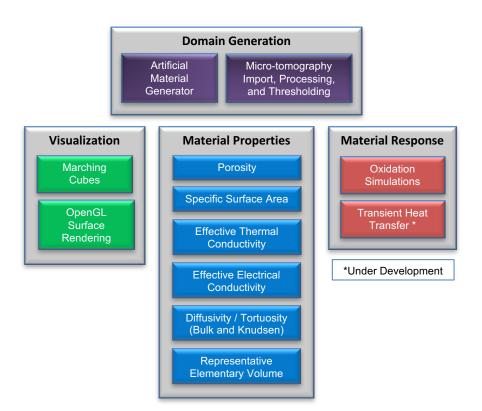
- 3D Fibers, 512³
- Intersecting, isotropic
- 0.6 porosity



Conclusion and Outlook



- Implemented finite difference and random walk tortuosity factor solvers into PuMA V2.1
- Demonstrated the necessity of using an isosurface collision detection for complex 3d media, a capability which currently only exists in PuMA
- Verified random walk model for tortuosity factors against Direct Simulation Monte Carlo (DSMC) simulations.
- Recommend changing current definitions of tortuosity factor to restore the value as a purely geometrical property.



Acknowledgements



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Questions?

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